



	Year 1 Addition and Subtraction
Objectives	Key Skills
 read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs represent and use number bonds and related subtraction facts within 20 add and subtract one-digit and two-digit numbers to 20, including zero solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = -9. 	 Read and write numbers to 100 in numerals, incl. 1—20 in words Recall bonds to 10 and 20, and addition facts within 20 Count to and across 100 Count in multiples of 1 2, 5 and 10 Solve simple 1-step problems involving addition, using objects, number lines and pictorial representations. Subtraction
Addition add, more, plus, and, put together, make, altogether, total, equal to, equals, double, most, count on, number line Subtraction equal to, take, take away, less, subtract, leaves, difference, how many more, how many fewer / less than, most, least, count back, how many left, how much less is_?	 Given a number, say one more or one less. Count to and over 100, forward and back, from any number. Represent and use subtraction facts to 20 and within 20. Subtract with one-digit and two-digit numbers to 20, including zero. Solve one-step problems that involve addition and subtraction, using concrete objects (ie bead string, objects, cubes) and pictures, and missing number problems. Read and write numbers from 0 to 20 in numerals and words.



	Year 1						
		Year 1 Addition					
	Concrete	Pictorial	Abstract				
Counting and adding more	Children add one more person or object to a group to find one more.	Children add one more cube or counter to a group to represent one more.	Use a number line to understand how to link counting on with finding one more.				
		One more than 4 is 5.	One more than 6 is 7. 7 is one more than 6. Learn to link counting on with adding more than one. 5 + 3 = 8				
Understanding part-part-whole relationship	understand the relationship with the whole.	Children draw to represent the parts and understand the relationship with the whole. The parts are 1 and 5. The whole is 6.	Use a part-whole model to represent the numbers. $6 + 4 = 10$ $6 + 4 = 10$				
	The parts are 2 and 4. The whole is 6.						



Knowing and finding number bonds within 10

Break apart a group and put back together to find and form number bonds.

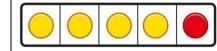


3 + 4 = 7

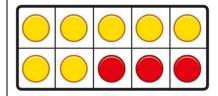


6 = 2 + 4

Use five and ten frames to represent key number bonds.

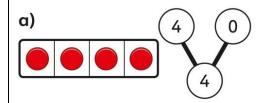


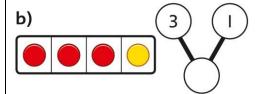
5 = 4 + 1



10 = 7 + 3

Use a part-whole model alongside other representations to find number bonds. Make sure to include examples where one of the parts is zero.





$$4 + 0 = 4$$

 $3 + 1 = 4$



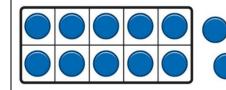
Understanding teen numbers as a complete 10 and some more

Complete a group of 10 objects and count more.



13 is 10 and 3 more.

Use a ten frame to support understanding of a complete 10 for teen numbers.

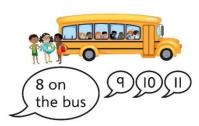


13 is 10 and 3 more.

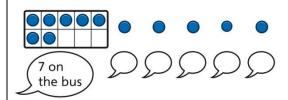
1 ten and 3 ones equal 13. 10 + 3 = 13

Adding by counting on

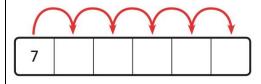
Children use knowledge of counting to 20 to find a total by counting on using people or objects.



Children use counters to support and represent their counting on strategy.



Children use number lines or number tracks to support their counting on strategy.



Adding the 1s

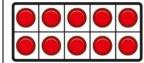
Children use bead strings to recognise how to add the 1s to find the total efficiently.



$$2 + 3 = 5$$

 $12 + 3 = 15$

Children represent calculations using ten frames to add a teen and 1s.



$$2 + 3 = 5$$

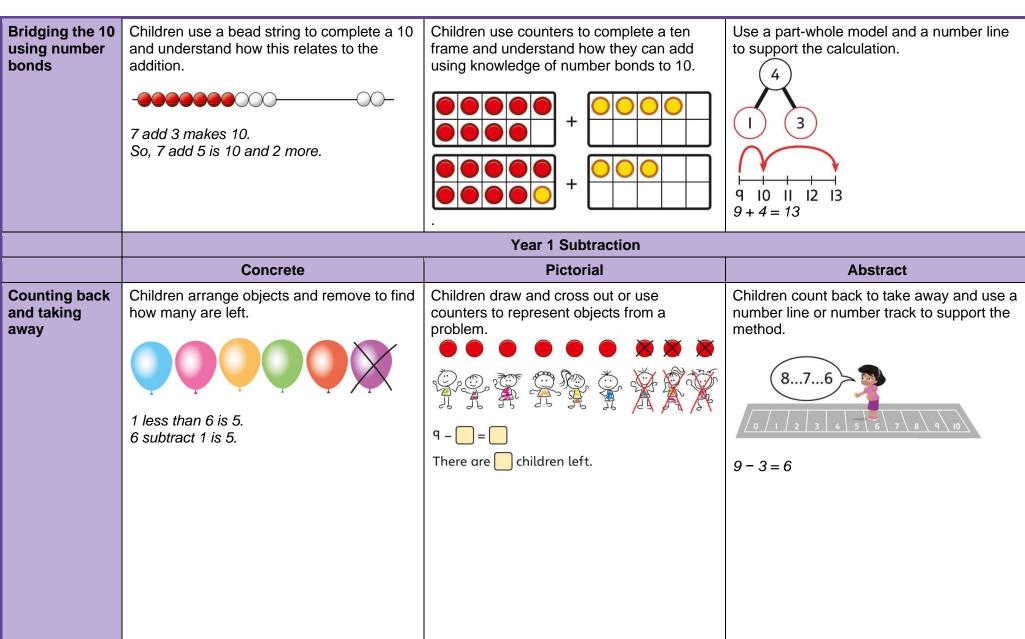
 $12 + 3 = 15$

Children recognise that a teen is made from a 10 and some 1s and use their knowledge of addition within 10 to work efficiently.

$$3 + 5 = 8$$

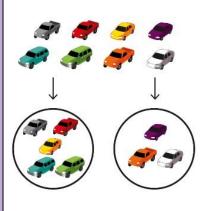
So, $13 + 5 = 18$





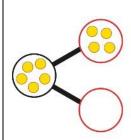


Finding a missing part, given a whole and a part Children separate a whole into parts and understand how one part can be found by subtraction.



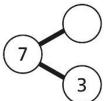
8 - 5 = ?

Children represent a whole and a part and understand how to find the missing part by subtraction.



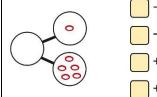
5 - 4 =

Children use a part-whole model to support the subtraction to find a missing part.



7 - 3 = ?

Children develop an understanding of the relationship between addition and subtraction facts in a part-whole model.

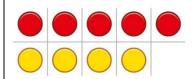


Finding the difference

Arrange two groups so that the difference between the groups can be worked out.



8 is 2 more than 6. 6 is 2 less than 8. The difference between 8 and 6 is 2. Represent objects using sketches or counters to support finding the difference.



5 - 4 = 1The difference between 5 and 4 is 1. Children understand 'find the difference' as subtraction.



10 - 4 = 6The difference between 10 and 6 is 4.



Subtraction within 20 Subtracting 10s and 1s

Understand when and how to subtract 1s efficiently.

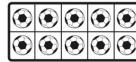
Use a bead string to subtract 1s efficiently.



$$5 - 3 = 2$$

 $15 - 3 = 12$

Understand when and how to subtract 1s efficiently.



$$5 - 3 = 2$$

 $15 - 3 = 12$

Understand how to use knowledge of bonds within 10 to subtract efficiently.

$$5 - 3 = 2$$

 $15 - 3 = 12$

For example: 18 - 12

Subtract 12 by first subtracting the 10, then the remaining 2.

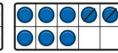


First subtract the 10, then take away 2.

For example: 18 - 12

Use ten frames to represent the efficient method of subtracting 12.





First subtract the 10. then subtract 2.

Use a part-whole model to support the calculation.



$$19 - 10 = 9$$

 $9 - 4 = 5$

Subtraction bridging 10 using number bonds

For example: 12 - 7

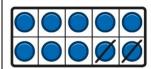
Arrange objects into a 10 and some 1s, then decide on how to split the 7 into parts.

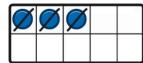




7 is 2 and 5, so I take away the 2 and then the 5.

Represent the use of bonds using ten frames.

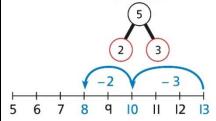




For 13 – 5, I take away 3 to make 10, then take away 2 to make 8.

Use a number line and a part-whole model to support the method.

13 - 5





Y	Year 1 Multiplication and Division				
Objectives	Key Skills				
 solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher. 	 Multiplication Count in multiples of 2, 5 and 10. Solve one-step problems involving multiplication, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher. Make connections between arrays, number patterns, and counting in twos, 				
Vocabulary	fives and tens. Begin to understand doubling using concrete objects and pictorial				
Multiplication	representations.				
groups of, lots of, times, array, altogether, multiply, count Division share, share equally, one each, two each, group, groups of, lots of, array	 Solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations arrays with the support of the teacher Through grouping and sharing small quantities, pupils begin to understand, division, and finding simple fractions of objects, numbers and quantities. They make connections between arrays, number patterns, and counting in twos, fives and tens. 				



	Year 1										
Year 1 Multiplication											
	Concrete Pictorial Abstract										
Recognising and making equal groups	Children arrange objects in equal and unequal groups and understand how to recognise whether they are equal. A B C	Children draw and represent equal and unequal groups. A B A A A A A A A A A A A A A A A A A	Three equal groups of 4. Four equal groups of 3.								
Finding the total of equal groups by counting in 2s, 5s and 10s	There are 5 pens in each pack 510152025303540	100 squares and ten frames support counting in 2s, 5s and 10s.	Use a number line to support repeated addition through counting in 2s, 5s and 10s. 10 10 10 10 10 10 10 10 10 10 10 10 10 1								



		Year 1 Division	
	Concrete	Pictorial	Abstract
Grouping	Learn to make equal groups from a whole and find how many equal groups of a certain size can be made.	Represent a whole and work out how many equal groups.	Children may relate this to counting back in steps of 2, 5 or 10.
	Sort a whole set people and objects into equal groups.	000000000	
		There are 10 in total. There are 5 in each group. There are 2 groups.	0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
	There are 10 children altogether. There are 2 in each group. There are 5 groups.		
Sharing	Share a set of objects into equal parts and work out how many are in each part.	Sketch or draw to represent sharing into equal parts. This may be related to fractions.	10 shared into 2 equal groups gives 5 in each group.



Year 2 Addition and Subtraction				
Objectives	Key Skills			
 solve problems with addition and subtraction: using concrete objects and pictorial representations, including those involving numbers, quantities and measures applying their increasing knowledge of mental and written methods recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 add and subtract numbers using concrete objects, pictorial representations, and mentally, including: a two-digit number and ones a two-digit number and tens a two two-digit numbers show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems. 	 Add a 2-digit number and ones (e.g. 27 + 6) Add a 2-digit number and tens (e.g. 23 + 40) Add pairs of 2-digit numbers (e.g. 35 + 47) and add three single-digit numbers (e.g. 5 + 9 + 7) Show that adding can be done in any order (the commutative law). Recall bonds to 20 and bonds of tens to 100 (30 + 70 etc.) Count in steps of 2, 3 and 5 and count in tens from any number. Understand the place value of 2-digit numbers (tens and ones) Compare and order numbers to 100 using < > and = signs. Read and write numbers to at least 100 in numerals and words. Solve problems with addition, using concrete objects, pictorial representations, involving numbers, quantities and measures, and applying mental and written methods. Subtraction Recognise the place value of each digit in a two-digit number. Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100. 			



Vocabulary

Addition

add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary

Subtraction

equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, how many fewer / less than, most, least, count back, how many left, how much less is_? difference, count on, strategy, partition, tens, units



		Year 2 Addition		
	Concrete	Pictorial	Abstract	
Understanding 10s and 1s	Group objects into 10s and 1s. Bundle straws to understand unitising of 10s.	Understand 10s and 1s equipment, and link with visual representations on ten frames.	using equipment or numerals. Tens Ones 3 2 =30+2= 32	
Adding 10s	Use known bonds and unitising to add 10s.	Use known bonds and unitising to add 10s.	Tens Ones 4 3 =40+3=43 Use known bonds and unitising to add 10s.	
	I know that $4 + 3 = 7$. So, I know that 4 tens add 3 tens is 7 tens.	I know that $4 + 3 = 7$. So, I know that 4 tens add 3 tens is 7 tens.	7 4 3 $4 + 3 = 7$ $4 tens + 3 tens = 7 tens$ $40 + 30 = 70$	



Adding a 1-digit number to a 2-digit number not bridging a 10

Add the 1s to find the total. Use known bonds within 10.

10





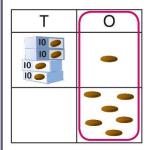






41 is 4 tens and 1 one. 41 add 6 ones is 4 tens and 7 ones.

This can also be done in a place value grid.



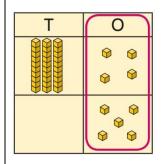
Add the 1s.







34 is 3 tens and 4 ones. 4 ones and 5 ones are 9 ones. The total is 3 tens and 9 ones.

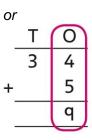


Add the 1s.

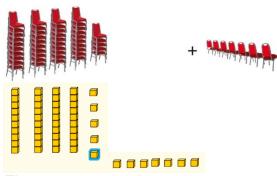
Understand the link between counting on and using known number facts. Children should be encouraged to use known number bonds to improve efficiency and accuracy.

This can be represented horizontally or vertically.

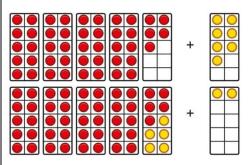
$$34 + 5 = 39$$



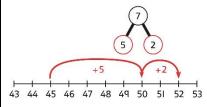
Adding a 1-digit number to a 2-digit number bridging 10 Complete a 10 using number bonds.



There are 4 tens and 5 ones. I need to add 7. I will use 5 to complete a 10, then add 2 more. Complete a 10 using number bonds.



Complete a 10 using number bonds.

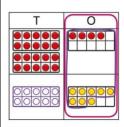


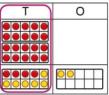
$$7 = 5 + 2$$

 $45 + 5 + 2 = 52$

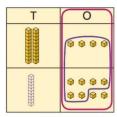


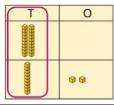
Adding a 1-digit number to a 2-digit number using exchange Exchange 10 ones for 1 ten.



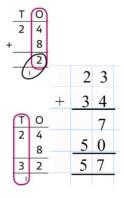


Exchange 10 ones for 1 ten.



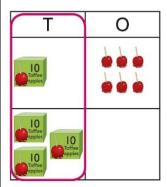


Exchange 10 ones for 1 ten.

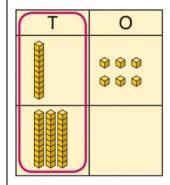


Adding a multiple of 10 to a 2-digit number using columns

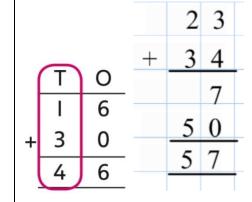
Add the 10s using a place value grid to support.



16 is 1 ten and 6 ones. 30 is 3 tens. There are 4 tens and 6 ones in total. Add the 10s using a place value grid to support.



16 is 1 ten and 6 ones. 30 is 3 tens. There are 4 tens and 6 ones in total. Add the 10s represented vertically. Children must understand how the method relates to unitising of 10s and place value.

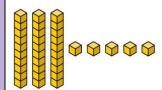


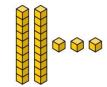
1 + 3 = 41 ten + 3 tens = 4 tens 16 + 30 = 46



Adding two 2-digit numbers

Add the 1s and then the 10s.





$$5+3=8$$

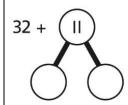
There are 8 ones in total.

$$3 + 2 = 5$$

There are 5 tens in total.

$$35 + 23 = 58$$

Add the 10s and 1s separately. Use a part-whole model to support.



$$11 = 10 + 1$$

$$32 + 10 = 42$$

$$42 + 1 = 43$$

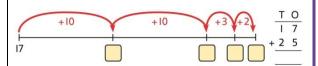
$$32 + 11 = 43$$



Year 2 Subtraction

Pictorial

Add the 10s and the 1s separately, bridging 10s where required. A number line can support the calculations.



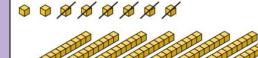
$$17 + 25$$

	2	3
+	3	4
		7
	5	0
	5	7

Subtracting multiples of 10

Use known number bonds and unitising to subtract multiples of 10.

Concrete

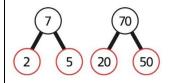


8 subtract 6 is 2. So, 8 tens subtract 6 tens is 2 tens. Use known number bonds and unitising to subtract multiples of 10.

100	
	30

10 - 3 = 7So, 10 tens subtract 3 tens is 7 tens. Use known number bonds and unitising to subtract multiples of 10.

Abstract



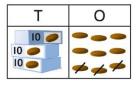
7 tens subtract 5 tens is 2 tens. 70 - 50 = 20



Subtracting a single-digit number

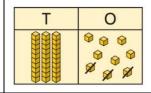
Subtract the 1s. This may be done in or out of a place value grid.



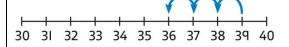


Subtract the 1s. This may be done in or out of a place value grid.



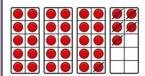


Subtract the 1s. Understand the link between counting back and subtracting the 1s using known bonds.



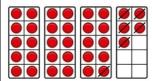
Subtracting a single-digit number bridging 10

Bridge 10 by using known bonds.



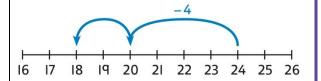
35 – 6 I took away 5 counters, then 1 more.

Bridge 10 by using known bonds.



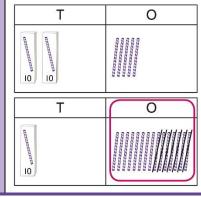
35 - 6 First, I will subtract 5, then 1.

Bridge 10 by using known bonds.

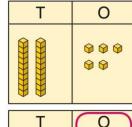


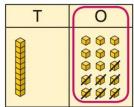
Subtracting a single-digit number using exchange

Exchange 1 ten for 10 ones. This may be done in or out of a place value grid.

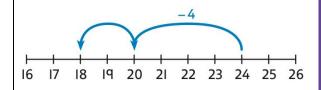


Exchange 1 ten for 10 ones.





Bridge 10 by using known bonds.





Subtracting a 2-digit number

61 - 18

I took away 1 ten and 8 ones.

Subtract the 1s. Then subtract the 10s. This may be done in or out of a place value grid.

Т	0
955550 955550	

•	•	•	•	•
•	lacksquare			

Subtract the 10s and the 1s.

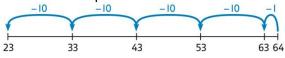
This can be represented on a 100 square.

1	2	3	4	5	6	7	8	9	10
П	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	148	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
qı	92	93	94	95	96	97	98	99	100

Subtract the 1s. Then subtract the 10s.

Subtract the 10s and the 1s.

This can be represented on a number line.

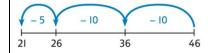


$$64 - 41 = ?$$

$$64 - 1 = 63$$

$$63 - 40 = 23$$

$$64 - 41 = 23$$

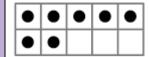


$$46 - 20 = 26$$

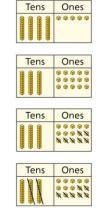
$$26 - 5 = 21$$

$$46 - 25 = 21$$

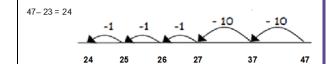
Subtracting a 2-digit number with exchange



Exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s.



Using number line. Partition the number into tens and ones. Count back in 1s or bridging through the tens number.





Year 2 Multiplication and Division					
Objectives	Key Skills				
 recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (x), division (÷) and equals (=) signs show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts. 	 Multiplication Count in steps of 2, 3 and 5 from zero, and in 10s from any number. Recall and use multiplication facts from the 2, 5 and 10 multiplication tables, including recognising odds and evens. Write and calculate number statements using the x and = signs. Show that multiplication can be done in any order (commutative). Solve a range of problems involving multiplication, using concrete objects, arrays repeated addition, mental methods, and multiplication facts. Pupils use a variety of language to discuss and describe multiplication. Division Count in steps of 2, 3, and 5 from 0 Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers. Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the x, ÷ and = signs. Show that multiplication of two numbers can be done in any order (commutative) 				
Vocabulary	and division of one number by another cannot.				
Multiplication groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative, sets of, equal groups, times as big as, once, twice, three times Division share, share equally, one each, two each, group, equal					
groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over					



	Year 2 Multiplication			
	Concrete	Pictorial	Abstract	
Equal groups and repeated addition	Recognise equal groups and write as repeated addition and as multiplication. 3 groups of 5 chairs 15 chairs altogether	Recognise equal groups using standard objects such as counters and write as repeated addition and multiplication. 3 groups of 5 15 in total	Use a number line and write as repeated addition and as multiplication. $ \begin{array}{cccccccccccccccccccccccccccccccccc$	
Using arrays to represent multiplication and support understanding	Understand the relationship between arrays, multiplication and repeated addition. 1111111111111111111111111111111111	Understand the relationship between arrays, multiplication and repeated addition. 4 groups of 5 5 groups of 5	Understand the relationship between arrays, multiplication and repeated addition. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	



Understanding commutativity

Use arrays to visualise commutativity.



I can see 6 groups of 3. I can see 3 groups of 6. Form arrays using counters to visualise commutativity. Rotate the array to show that orientation does not change the multiplication.



This is 2 groups of 6 and also 6 groups of 2.

Use arrays to visualise commutativity.





4+4+4+4+4=20 5+5+5+5=20 $4 \times 5 = 20$ and $5 \times 4 = 20$



Learning ×2, ×5 and ×10 table facts

Develop an understanding of how to unitise groups of 2, 5 and 10 and learn corresponding times-table facts.







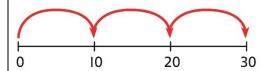
3 groups of 10 ... 10, 20, 30 $3 \times 10 = 30$

Understand how to relate counting in unitised groups and repeated addition with knowing key times-table facts.





00000000



$$10 + 10 + 10 = 30$$

 $3 \times 10 = 30$

Understand how the times-tables increase and contain patterns.



I × I0 =

2 × 10 =

3 × 10 = 4 × 10 =

5 × 10 =

$$8 \times 10 = \boxed{}$$

$$9 \times 10 = \boxed{}$$

10 ×	10 =	

$$5 \times 10 = 50$$

$$6 \times 10 = 60$$



	Year 2 Division			
	Concrete	Pictorial	Abstract	
Sharing equally	Start with a whole and share into equal parts, one at a time.	Represent the objects shared into equal parts using a bar model.	Use a bar model to support understanding of the division.	
	000000000	20 shared into 5 equal parts.	18 ÷ 2 = 9	
	12 shared equally between 2. They get 6 each.	There are 4 in each part.	10.2-0	
	Start to understand how this also relates to grouping. To share equally between 3 people, take a group of 3 and give 1 to each person. Keep going until all the objects have been shared			
	15			
	They get 5 each.			
	15 shared equally between 3. They get 5 each.			





Understand how to make equal groups from a whole.





8 divided into 4 equal groups. There are 2 in each group.

Understand the relationship between grouping and the division statements.





 $12 \div 4 = 3$



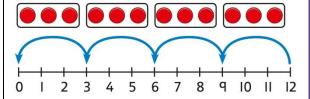
 $12 \div 6 = 2$



 $12 \div 2 = 6$



Understand how to relate division by grouping to repeated subtraction.



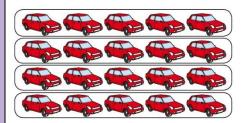
There are 4 groups now.

12 divided into groups of 3. $12 \div 3 = 4$

There are 4 groups.

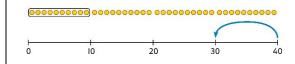
Using known times-tables to solve divisions

Understand the relationship between multiplication facts and division.



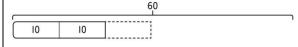
4 groups of 5 cars is 20 cars in total. 20 divided by 4 is 5.

Link equal grouping with repeated subtraction and known times-table facts to support division.



40 divided by 4 is 10.

Use a bar model to support understanding of the link between times-table knowledge and division.



Relate times-table knowledge directly to division.

$$1 \times 10 = 10$$
$$2 \times 10 = 20$$

 $3 \times 10 = 30$ $4 \times 10 = 40$

 $5 \times 10 = 50$

 $6 \times 10 = 60$ $7 \times 10 = 70$

 $8 \times 10 = 80$

I used the I0 times-table to help me.
$$3 \times 10 = 30$$
.

I know that 3 groups of 10 makes 30, so I know that 30 divided by 10 is 3.

$$3 \times 10 = 30$$
 so $30 \div 10 = 3$